# Output substitution in multi-species trawl fisheries: 

# implications for quota setting 

Trond Bjorndal

Phoebe Koundouri ${ }^{1}$

Sean Pascoe

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#### Abstract

In most multi-species fisheries managed through output controls, total allowable catches (TACs) are set primarily on the basis of biological considerations, usually on a species by species basis. An implicit assumption of management is that fishers are able to adjust their product mix in line with these quotas. If this is not the case, then over-quota catch occurs, leading to either illegal landings or discards. In either case, the effectiveness of the TAC in conserving the resource is reduced. In this paper we show that in the case of multi-species fisheries that exhibit jointness in production, setting TACs on an individual species' basis is inappropriate. In particular, we quantify technical interactions through the estimation of a multi-output distance function for the UK North Sea beam and otter trawl fisheries, and find that in most cases, the potential of substitutability between the main and alternative species is relatively small. We argue that failure to quantify and integrate these technical interactions in the construction of management instruments for fisheries regulation, may result in increased discarding, illegal fishing and potentially lower than expected future yields.


Key Words: multi-output fishery, multi-output distance function, elasticities of substitution, efficiency.

JEL: Q22

## Introduction

The need for fisheries management has been accepted in most countries around the world, and relatively few completely unregulated fisheries exist within the fishing zones of coastal states. Fisheries regulation varies considerably, ranging from basic limited entry to complex individual transferable quota programs. The failure of input controls to effectively regulate fishing activity as a consequence of input substitution (i.e. of unregulated inputs for restricted inputs) has resulted in many countries either fully adopting an output control system (e.g. New Zealand), or some combination of input and output controls.

Fundamental to the use of output controls is the establishment of a total allowable catch (TAC). This may be either fished competitively - a strategy often criticised by economists due to the incentive to race to fish and the consequent dissipation of resource rent - or allocated to fishers as individual quotas (transferable or non-transferable). While in theory TACs are set on the basis of the multiple objectives of fisheries management, in practice TACs are primarily set on the basis of biological considerations, namely the state of the fish stocks. In Europe, advice on TACs is provided by the International Council for the Exploitation of the Seas (ICES) based on stock assessments of the individual species. Although some recognition is given to some biological interaction (e.g. predator-prey relationships), TACs are set for species individually. Similar TAC setting procedures are employed in other countries using output controls.

In multi-species fisheries, the ability of the fisher to target individual species is generally assumed to be limited as output is characterised by joint production. The catch composition is a function of the type of gear employed and the relative abundance of the different species in the different areas or times fished. If the relative abundance of the different species does not
vary substantially from area to area, then the ability of the fisher to change their catch composition through changing fishing area is limited.

Management through TACs set on an individual species basis involves an implicit assumption that fishers are able to adjust their behaviour sufficiently such that the catch composition reflects the set of TACs. If fishers are unable to adjust their catch composition, then there exists the likelihood of over-quota catch, leading to either illegal landings or discarding. In either case, the integrity of the TAC is violated, and the conservation objectives are not achieved. In contrast, setting TACs taking into account the likely output mix of the fishery may result in a more efficient use of the resource.

In this paper, the potential for fishers to alter their targeting behaviour is examined using a multi-output distance function approach. This allows the estimation of the elasticity of substitution between various outputs. The analysis is applied to two fleet segments operating in the North Sea. In each case, the stocks of one or more species caught by these fleet segments is in decline, and TACs for these species have been set at a low level with the expectation that this will result in stock recovery. If fishers are unable to change their catch composition to avoid these species, it is likely that these TACs will be violated and the potential for a rapid stock recovery reduced.

The paper is organised as follows. The next section reviews previous studies involving the estimation production functions in fisheries and the treatment of multiple outputs. Then a description is provided of the methodology employed in the study, and the econometric specification of the model employed. After this, a description of the fishery examined and the data used in the analysis is presented. This is followed by the empirical results of the analysis,
including the estimates of the elasticities of output substitution. Finally, the policy implications of the analysis are presented.

## Single vs multi-output production functions in fisheries

A production function defines the relationship between the level of inputs and the resultant level of outputs. It is estimated from observed outputs and input usage and indicates the average level of outputs for a given level of inputs (Schmidt). In fisheries, several studies have estimated production functions at either the individual boat level or aggregate fishery level (e.g. Hannesson, Bjørndal, Campbell and Lindner, Squires, Pascoe and Robinson). The objective of these studies was generally to estimate output elasticities associated with each input, and in some cases the potential for input substitution.

More recently, emphasis has shifted to the estimation of production frontiers. Interest in technical efficiency has largely driven this shift, although there are theoretical reasons why the estimation of production frontiers has advantages over the estimation of production functions (see Kumbhakar). Only limited attempts to estimate stochastic production frontiers for fisheries have been undertaken ${ }^{1}$.

A common feature of these studies is the reliance on a single measure of output. This approach has been common for the estimation of production functions in most industries. However, unlike many other industries, many fisheries are characterized by joint production. Joint production occurs when firms produce several outputs at the same time. In fisheries, this is due to technological aspects of the production process, in particular technical interdependencies and non-allocable inputs. Resource jointness in fisheries can arise as a result of several reasons. In particular, many species are often found in the same geographical
area and will be harvested at the same time as a result of the limited selectivity of the fishing gear.

The use of a singe composite measure of output under such circumstances imposes a number of restrictive assumptions. Adding up the weight of each output assumes that all species are equally important in the catch, which is clearly not the case as high volume species tend to be low value. This can be overcome through incorporating prices into the analysis, and several studies have used revenue as the output measure (e.g. Sharma and Leung, Pascoe and Coglan, Herrero and Pascoe). The use of total revenue as the output measure requires the assumption that output prices do not differ between firms, and changes in 'output' due to changes in price need to be compensated for. A further method that has been applied (e.g. Pascoe, Andersen and de Wilde) has been to weight the quantity of each output on the basis of its revenue share. This avoids the biases introduced through using prices only, but assumes revenue maximizing behavior and competitive output markets - assumptions that may not be realistic in many instances. Moreover, an aggregate production function imposes the restrictive assumption of separability in inputs and output on the transformation function. This implies that the input mix can be changed significantly without affecting the slope of the production possibility curve, and that marginal costs depend only on the output mix, and are thus independent of the input prices.

An alternative to single output measures is the use of multi-output measures. Several studies have been undertaken assessing technical efficiency and capacity utilization using Data Envelopment Analysis (DEA) in fisheries (see, for example, Feltoven; Pascoe, Coglan and Mardle; Tingley, Pascoe and Mardle; Vestergaard, Squires and Kirkley). A key feature of DEA is that it is directly able to incorporate multiple outputs into the analysis. However, as it
is non-parametric, it is sensitive to random error, and also does not provide estimates of the impact of individual inputs on the level of outputs, or the relationship between the outputs themselves.

Alvarez and Orea examined two methods for incorporating multi outputs in fisheries production functions and compared these with single output measures. The first method - the multi-output production function - involved regressing one (of two) outputs against the other output and set of inputs. The second method - the output oriented distance function involved a normalized and restricted model that considers the maximal proportional expansion of the output vector given an input vector. Both methods were found to produce similar output elasticities associated with each input, and these were similar to those derived through the single output production function. Moreover, the specification of the multi-output production process overcame the problems associated with the implicit assumptions imposed through the different aggregation processes necessary to derive the single composite output measure.

Fousekis compared the multi-output distance function with the stochastic ray function approach. He found that that latter technique generally resulted in lower efficiency scores, although both methods produced consistent rankings of the efficiency scores. The different techniques also resulted in different estimates of the key production elasticities that are relevant for policies aiming at reduction of harvests through individual input controls.

A key criticism of the multi-output production function is that the output selected as dependent variable plays an asymmetric role, which affects the estimated parameters of the production technology as well as the relevant efficiency score. In contrast, in the output
oriented distance function, every output plays the same role, avoiding the asymmetry problem (i.e., the efficiency measures are not output specific but radial). Further, the output oriented distance function has advantages over the other methods in that estimation is possible without separability and jointness, and information on prices is not required. However, estimation of the distance function requires the assumption of linear homogeneity in outputs, implicitly implying that not only efficiency, but also noise is radial. That is, the influence of noise on one output is the same as that upon another output. This notwithstanding, the output-oriented distance function appears to be the most appropriate method for estimating multi-output production processes.

## The Restricted Multi-Output Distance Function

The methodology employed in the study largely follows that used by Fare and Grosskopf; Grosskopf et al.; Coelli and Perelman and Morrison Paul et al.. These studies largely derive from the initial distance function theory developed by Shephard (1970). Given the existence of a production possibility frontier, the distance that any producer is away from the frontier is a function of the set of inputs used, $\mathbf{x}$, and the level of outputs produced, $\mathbf{y}$. For the outputoriented model, this can be expressed as

$$
\begin{equation*}
D(\mathbf{x}, \mathbf{y})=\min \{\theta:(\mathbf{y} / \theta) \in P(\mathbf{x})\} \tag{1}
\end{equation*}
$$

where $D(\mathbf{x}, \mathbf{y})$ is the distance from the firm's output set to the frontier, and $\theta$ is the corresponding level of efficiency. The output distance function seeks the largest proportional increase in the observed output vector $\mathbf{y}$ provided that the expanded vector $(\mathbf{y} / \theta)$ is still an element of the original output set (Grosskopf et al.). ${ }^{2}$ If the firm is fully efficient, so that it is
on the frontier, $D(\mathbf{x}, \mathbf{y})=\theta=1$, whereas $D(\mathbf{x}, \mathbf{y})=\theta<1$ indicates that the firm is inefficient. The output distance function is homogeneous of degree one in outputs (Shephard1970). ${ }^{3}$

Fishery models recognize that capital (the vessel) is usually a fixed factor, due to limited second hand markets and high adjustment costs. In this case a restricted profit function is appropriate, where the fishing vessel is assumed to maximize profits by choosing inputs and harvest level subject to the size of the vessel used in harvesting. Modeling fishermen behavior with profit functions, however, is appropriate only when the output quantities are choice variables. For fishing vessel in individual vessel quota (IVQ) regulated fisheries ${ }^{4}$ the harvest level is set by the individual quota and is no longer a choice variable, i.e., harvest is an exogenous or restricted factor. Hence the price-taking fishermen maximizes profits for a given harvest level $H_{i t}$, or equivalently, minimizes the cost of harvesting the given quota, assuming the quota is the only fixed factor (Asche et al.).

The restricted profit maximization problem can be written as:

$$
\begin{align*}
& \Pi_{i t}^{R}\left(p_{t}^{P}, p_{t}^{S}, p_{t}^{C}, p_{t}^{A}, p_{t}^{O}, p_{t}^{K}, p_{t}^{E}\right)= \\
& \max \left(p_{t}^{P} \cdot y_{i t}^{P}+p_{t}^{S} \cdot y_{i t}^{S}+p_{t}^{C} \cdot y_{i t}^{C}+p_{t}^{A} \cdot y_{i t}^{A}+p_{t}^{O} \cdot y_{i t}^{O}\right)-C_{i t}\left(Y_{i t}, p_{t}^{E}, p_{t}^{K}\right) \tag{2}
\end{align*}
$$

where

$$
\begin{equation*}
C_{i t}\left(Y_{i t}, p_{t}^{E}, p_{t}^{K}\right)=\min p_{t}^{E} \cdot x_{i t}^{E}+p_{t}^{K} \cdot x_{i t}^{K}: H_{i t}\left(Y_{i t}, x_{i t}^{E}, x_{i t}^{K}\right)=0 \tag{3}
\end{equation*}
$$

To anticipate the empirical estimation, the relevant variables are introduced. The vessel and time specific restricted profit function and the cost function are ? ${ }^{R}{ }_{i t}($.$) and C_{i t}($.$) , respectively.$ Outputs are plaice $\left(y^{P}{ }_{i t}\right)$, sole $\left(y^{S}{ }_{i t}\right), \operatorname{cod}\left(y^{C}{ }_{i t}\right)$, anglerfish $\left(y^{A}{ }_{i t}\right)$ and other $\left(y^{O}{ }_{i t}\right) ; p^{P}{ }_{t} p^{S}{ }_{t} p^{C}{ }_{t} p^{A}{ }_{t}$ and $p^{o}{ }_{t}$, are the respective competitive market prices. Input price vectors for labour (days employed in fishing), $x^{E}{ }_{i t}$ and capital $x^{K}{ }_{i t}$, are $p^{E}{ }_{t}$ and $p^{K}{ }_{t}$, respectively. $\mathbf{Y}_{i t}$ is vessel (i) and time
( $t$ )-specific aggregate harvest quantity. By solving for optimal levels of output, one can therefore find the potential rents in such a fishery. ${ }^{5}$

Given the advantages of the distance function discussed above, we model fishing behavior through a restricted multi-output distance function. The production technology is defined by output sets, $\mathrm{P}\left(\mathbf{X}_{\mathrm{it}} ; \mathbf{H}_{\mathrm{it}}\right)$, which represents the set of all output vectors, $\mathbf{Y}_{\mathrm{it}}$, which can be produced using the input vector, $\mathbf{X}_{\mathrm{it}}$, given that individual fishermen decide the mix of input quantities for a given quota (which can be vessel (i) and time $(t)$ specific). Quotas restrict the harvest level $\mathbf{H}_{\mathrm{it}}$. That is,

$$
\begin{equation*}
P\left(\boldsymbol{X}_{i t} ; \boldsymbol{H}_{i t}\right)=\left\{\boldsymbol{Y}_{i t}: \boldsymbol{X}_{i t} \text { can produce } \boldsymbol{Y}_{i t} \text { given } \boldsymbol{H}_{i t}\right\} \tag{4}
\end{equation*}
$$

For each $\mathbf{X}_{\mathrm{it}}$, the output set $\mathrm{P}\left(\mathbf{X}_{\mathrm{it}} ; \mathbf{H}_{\mathrm{it}}\right)$ is assumed to satisfy the properties mentioned above. The output distance function is defined on the output set, $\mathrm{P}\left(\mathbf{X}_{\mathrm{it}} ; \mathbf{H}_{\mathrm{it}}\right)$, as:

$$
\begin{equation*}
D_{i t}^{R}\left(x_{i t}^{E}, x_{i t}^{K}, y_{i t}^{P}, y_{i t}^{S}, y_{i t}^{C}, y_{i t}^{A}, y_{i t}^{O} ; H_{i t}\right)=\min \left\{\theta_{i t:}:\left(Y_{i t} / \theta_{i t}\right) \in P\left(X_{i t} ; H_{i t}\right)\right\} \tag{5}
\end{equation*}
$$

where $D_{i t}^{R}($.$) , the restricted output distance function, is non-decreasing in outputs and$ increasing in inputs, linearly homogeneous in outputs, $D_{i t}^{R}()=$.1 and $D_{i t}^{R}()=$.1 if $\mathbf{Y}_{\text {it }}$ belongs to the "frontier" of the production possibility set; ? ${ }_{i t}$ measures the proportional (radial) expansion of the output vector that brings the ith firm to the efficient frontier. ${ }^{6}$

Shephard $(1953,1970)$ has shown that the output distance function may also be obtained as a profit maximal profit function. This means that equation (5) can alternatively be written as:

$$
\begin{align*}
& D_{i t}^{R}\left(x_{i t}^{E}, x_{i t}^{K}, y_{i t}^{P}, y_{i t}^{S}, y_{i t}^{C}, y_{i t}^{A}, y_{i t}^{O} ; H_{i t}\right)= \\
& \max _{p^{d}}\left(p_{t}^{p} y_{i t}^{p}+p_{t}^{S} y_{i t}^{S}+p_{t}^{C} y_{i t}^{C}+p_{t}^{A} y_{i t}^{A}+p_{t}^{o} y_{i t}^{o}: \coprod_{i t}^{R}(.)\right\} m=1, \ldots, 6 \tag{6}
\end{align*}
$$

## Econometric Specification

In order to estimate the distance from the frontier, both the frontier itself and the relationship between inputs and outputs need to be determined. This requires some form of multi-output production function $P(\mathbf{x})$ to be specified. The most common functional form applied is the translog production function, as it does not impose restrictive assumptions regarding substitutability between inputs (and in this case outputs). This is particularly important in this study as a primary objective is to assess the elasticity of substitution between outputs.

The translog distance function with $\mathrm{M}(m=1,2, \ldots, M)$ outputs and $\mathrm{K}(k=1,2, \ldots, K)$ inputs, and for $\mathrm{I}(i=1,2, \ldots, I)$ firms, can be given by:

$$
\begin{align*}
\ln D_{i} & =\alpha_{0}+\sum_{m} \alpha_{m} \ln y_{m i}+0.5 \sum_{m} \sum_{n} \beta_{m n} \ln y_{m} \ln y_{n i} \\
& +\sum_{k} \alpha_{k} \ln x_{k, i}+0.5 \sum_{k} \sum_{l} \beta_{k l} \ln x_{k} \ln x_{l i}  \tag{7}\\
& +\sum_{k} \sum_{m} \beta_{k m} \ln x_{k i} \ln y_{m i}
\end{align*}
$$

In order to maintain the homogeneity conditions, a number of restrictions need to be imposed. These conditions involve the constraints $\sum_{m} a_{m}=1, \sum_{n} \beta_{m n}=\sum_{m} \beta_{k m}=0$, while symmetry restrictions require $\beta_{m n}=\beta_{n m}$ and $\beta_{k l}=\beta_{l k}$. The homogeneity restrictions can be imposed through normalizing the function by one of the outputs. This results in:

$$
\begin{align*}
\ln D_{i} / y_{1 i} & =\alpha_{0}+\sum_{m} \alpha_{m} \ln \left(y_{m i} / y_{1 i}\right)+0.5 \sum_{m} \sum_{n} \beta_{m n} \ln \left(y_{m} / y_{1 i}\right) \ln \left(y_{n i} / y_{1 i}\right) \\
& +\sum_{k} \alpha_{k} \ln x_{k, i}+0.5 \sum_{k} \sum_{l} \beta_{k l} \ln x_{k} \ln x_{l i}  \tag{8}\\
& +\sum_{k} \sum_{m} \beta_{k m} \ln x_{k i} \ln \left(y_{m i} / y_{1 i}\right)
\end{align*}
$$

The level of inefficiency can be estimated from a stochastic frontier production function of the form $\mathbf{y}=\mathrm{f}(\mathbf{x})+\mathrm{v}-\mathrm{u}$, where $v$ is the error term, assumed to be $\mathrm{N}[0, \sigma]$, and $u$ is the one sided inefficiency term that may take one of several distributional forms. The level of efficiency is estimated as the exponent of the negative of the error term, i.e., $\exp (-u)$. Consequently, $\ln D_{i}=-u_{i}$, and the normalized equation can be expressed as

$$
\begin{align*}
-\ln y_{1 i} & =\alpha_{0}+\sum_{m} \alpha_{m} \ln \left(y_{m i} / y_{1 i}\right)+0.5 \sum_{m} \sum_{n} \beta_{m n} \ln \left(y_{m} / y_{1 i}\right) \ln \left(y_{n i} / y_{1 i}\right) \\
& +\sum_{k} \alpha_{k} \ln x_{k, i}+0.5 \sum_{k} \sum_{l} \beta_{k l} \ln x_{k} \ln x_{l i}  \tag{9}\\
& +\sum_{k} \sum_{m} \beta_{k m} \ln x_{k i} \ln \left(y_{m i} / y_{1 i}\right)+v_{i}+u_{i}
\end{align*}
$$

For estimation purposes, the negative sign on the dependent variable can be ignored (i.e., we use $\ln y_{l}$ rather than $-\ln y_{l}$ ). This results in the signs of the estimated coefficients being reversed, but is more consistent with the expected signs of conventional production functions (Coelli and Perelman), and provides a convenient means of qualitatively assessing the models.

In order to separate the stochastic and inefficiency effects in the model, a distributional assumption has to be made for $u_{i}$. Two main distributional assumptions that have been proposed are a normal distribution truncated at zero, $u_{j} \sim\left\lfloor N\left(\mu, \sigma_{u}^{2}\right)\right\rfloor$ (Aigner, Lovell and Schmidt), and a half-normal distribution truncated at zero, $u_{j} \sim\left[N\left(0, \sigma_{u}^{2}\right)\right]$ (Jondrow et al.). In addition, the inefficiency can also be considered to have a time invariant component, so
that $u_{i, t}=u_{i} \exp [\eta(T-t)]$ (Battese and Coelli), where $T$ is the terminal time period (i.e., $u_{i, t}=u_{i}$ when $\left.t=T\right)$.

Following Grosskopf et al., the Allen elasticities of substitution can be directly derived from the distance function, given by

$$
\begin{equation*}
A_{y y^{\prime}}(x, y)=\left[D(x, y) * \frac{\partial^{2} D(x, y)}{\partial y \partial y^{\prime}}\right] /\left[\frac{\partial D(x, y)}{\partial y} * \frac{\partial D(x, y)}{\partial y^{\prime}}\right] \tag{10}
\end{equation*}
$$

where $A_{y y}$, is the Allen elasticity of substitution between output y and y '. A negative value indicates the outputs are substitutes, while a positive value indicates complementarity. The size of the value is a measure of the strength of the substitute/complementarity relationship.

In order to estimate the values of the first and second order derivatives, the values of $\alpha$ and $\beta$ relating to the output over which the production function was normalized need to be derived. This can be done by using the homogeneity restrictions that were imposed on the model. For the purposes of estimating the elasticity of substitution, the signs of the estimated coefficients need to be reversed.

## The UK North Sea Demersal fishery

The North Sea contains a number of interacting multi-species fisheries of great importance to many countries (Figure 1). The North Sea is the major fishing area in European Community waters. Over half of the combined total allowable catches of all species in all EU waters are taken from the North Sea. Commercial activity in the region is mostly undertaken by fishermen from the UK, Denmark, the Netherlands, France, Germany, Belgium and Norway.

Transboundary stocks are shared between the EU and Norway. Based on the total allowable catches (TACs) and the guide prices for each species, the total value of the allowable catch in 1999 was estimated to be about 1.5 billion Euro (Table 1). This is an underestimate of the true value of landings as the guide prices are generally lower than market prices. However, it provides an indication of the order of magnitude of the value of the fishery.

This study focuses on two main fleet segments that make up the majority of the UK North Sea demersal fleet: the UK beam trawl and the English otter trawl fleet segments.

The UK North Sea beam trawl fleet targets primarily high value flatfish (particularly sole and plaice), but also catches a considerable quantity of cod and anglerfish. In addition, many other species are caught as bycatch in varying, but small, quantities. Most of the stocks exploited by the fleet are heavily over-fished, resulting in a substantial decrease in quota levels over recent years. In addition, the fishery has been targeted for decommissioning as it is considered to have considerable excess capacity. Fleet size has been almost halved between 1994 and 2000 as a result of the reduced North Sea quotas, pushing some boats into the English Channel and/or Celtic Sea, and decommissioning.

The English otter trawlers primarily target cod, haddock, saithe and whiting, but also catch plaice and nethrops. These species comprise 90 per cent of the catch by volume, and a greater proportion by value. In addition, a range of other species is caught as bycatch.

The key species caught by both groups are subject to quota controls under the European Common Fisheries Policy. Prior to 1998, quota was allocated to the producer organizations (POs) to which the trawlers belonged, based on the rolling track record of the member
vessels. This would increase or decrease with the actual catch of the individuals, although the POs were expected to attempt to keep the total catch within the allocation. Different POs ran different schemes, with some operating an individual transferable quota (ITQ) system (with trade limited to within the PO ) and others operating a more competitive TAC system. For the fleet segments examined, most beam trawlers were managed under effectively an ITQ scheme, while most otter trawlers were managed under a pooled quota system. In 1999, the track record system was changed to a fixed quota allocation (FQA). Despite being 'fixed', these could be traded by individuals, either through an annual lease, or through more permanent arrangements (although the process for the latter was generally administratively complex, inhibiting 'permanent' transfers).

Despite being subject to quota controls, the quotas were not binding over the period examined. Since the introduction of the FQAs in 1999, the only binding quotas for North Sea species were for saithe and sole in 2000 . For most species, quota uptake ranged between 70 and 90 per cent (DEFRA). An analysis of the available beam trawl logbook and quota allocation data for 2000 (see below) found that over 75 per cent of the vessels did not fill their quota allocation, with the remainder exceeding the allocation (presumably through quota leasing). Given the apparent abundance of quota and the apparent effectiveness of the quota leasing market, it was assumed for the purposes of this study that the quotas were not effectively constraining output.

## The Available Data

Logbook production data and boat characteristics information from the central fleet registry for the beam and otter trawlers operating in the North Sea were used in the analysis. The data available for the otter trawl fleet relates only to the boats in the fleet registered to English
ports. Data on Scottish otter trawlers are held separately, and were not available for this analysis. ${ }^{7}$ The logbook data were available on a monthly basis over the 11 year-period 19902000.

Over the period, data were available for 58 beam trawlers, although only between 30 and 40 operated in any one year, and 152 otter trawlers, with between 100 and 120 operating in any one year. For both groups, only boats that were still registered in 2000 were included. As noted above, many boats had left the fishery as a result of decommissioning. The boats that left the fishery though the decommissioning scheme were most likely the least efficient, and their inclusion in the earlier years of the analysis (but not the later years) might have affected the results. Hence, for consistency, the target population was defined in terms of those boats that were registered in 2000. A second condition was imposed that the boats must have operated in the fishery in at least three of the 11 year data period.

The data set was also subject to further exclusions. For beam trawlers, boats that primarily targeted brown shrimp (Crangon crangon) were excluded. For these boats, the catch of the other species considered was negligible, and the fishing operation was considered sufficiently different to exclude from the analysis. Of the remaining vessels, not all boats recorded catch of the key species (plaice) in each year. As this formed the dependent variable in the model, boats that did not record landings of plaice were excluded for that year. Again, boats that did not have catches for at least three years after removing observations without plaice were excluded from the analysis. Similarly for the otter trawlers, boats that did not record landings of cod (the main species) were excluded. As with the beam trawl data, boats that did not have data for at least three years after removing observations without cod were excluded from the analysis. The key characteristics used in the analysis are presented in tables 2 and 3. In most
years, data were available for between 30 and 40 beam trawlers, and between 100 and 120 otter trawlers.

Catches of the key species used in the model varied over the period examined, largely as a result of changes in stock conditions. The key species were selected on the basis of both weight and contribution to total value and constituted 90 per cent of the value of total catch. The remaining species were aggregated into and 'other' category using a divisia index approach.

While several physical characteristics were available in the data set, e.g. length, vessel capacity units and width, only engine power $(\mathrm{kW})$ was used in the model. Boat deck area (expressed as the product of length and width) was found to be highly correlated with engine power ( $\mathrm{r}=0.94$ ), while vessel capacity units are a composite measure of both boat size and engine power (and, thus, was also highly correlated with engine power). The number of days at sea was also used as a variable in the model, representing the level of capital utilization.

Stock information for the key species examined was available on an annual basis (ICES). Stock indexes were derived based on the total available biomass in each year (with the base year being 1990). Changes in the stock abundance over the period of the data are illustrated in Figure 2. As can be seen, the different species were subject to differing changes in stock abundance. For the 'other' species, average catch per day fished across the fleet was used to derive the stock index. This approach implicitly assumes that catch per day fished is proportional to the available stock abundance. Individual stock information on many of the species in the 'other' category was not available.

Accounting for variations in stock abundance in fisheries production functions is generally undertaken through either the direct inclusion of the stock, or through the use of dummy variables. A particular problem exists for the use of stock indexes in multi-output production functions in that each stock measure relates directly to only one of the outputs, although indirectly it may affect the output of the others by affecting fishing patterns. A composite stock variable cannot effectively capture the stock changes of the different species, which do not follow a consistent pattern. Use of dummy variables is also problematic, as a single annual dummy variable cannot adequately represent the different individual stock effects. A series of individual stock dummy variables run into the same problems as the stock indexes, in that they cannot be related to any particular stock. In this study, a further problem was experienced, in that the stock indexes were highly correlated. For example, for the beam trawl fishery, the sole and plaice stock indexes had a correlation coefficient of 0.90 , while plaice and 'other' species had a correlation coefficient of 0.80 . Initial attempts at incorporating the stock indexes fully into the translog framework resulted in a singular matrix due to the high level of multicollinearity.

To overcome these problems, the catches in each time period were normalized using the stock indexes, i.e., the catch in each time period was divided by the stock index in that time period. This allows the effects of changes in stock size on catch to be incorporated into the analysis, but imposes the implicit assumption of unitary output elasticity with respect to stock size. This assumption is most likely valid given the nature of the resources, in that they are widely dispersed, fairly uniform in density across their areas of distribution and exploited across their whole areas of distribution.

## Empirical Results

The adjusted catches of each species were normalized by plaice and cod for the beam trawl and the otter trawl, respectively, in order to estimate the multi-output production frontier. The data were further normalized by the mean value of each variable, such that the average value of the normalized data was equal to one. This allows the output elasticities with respect to the outputs of the other species and the inputs to be determined directly from the results of the analysis as the $\alpha$ coefficients.

The models were estimated using FRONTER 4.1 (Coelli). A series of tests can be conducted to examine the specification of the models. These are tested through imposing restrictions on the model and using the generalized likelihood ratio statistic $(\lambda)$ to determine the significance of the restriction. The generalized likelihood ratio statistic is given by $\lambda=-2\left[\ln \left\{L\left(H_{0}\right)\right\}-\ln \left\{L\left(H_{1}\right)\right\}\right]$, where $\ln \left\{L\left(H_{o}\right)\right\}$ and $\ln \left\{L\left(H_{l}\right)\right\}$ are the values of the loglikelihood function under the null $\left(H_{o}\right)$ and alternative $\left(H_{l}\right)$ hypotheses. The restrictions form the basis of the null hypothesis, with the unrestricted model being the alternative hypothesis. The value of $\lambda$ has a $\chi^{2}$ distribution with the number of degrees of freedom given by the number of restrictions imposed.

A key test is the one-sided generalized likelihood ratio-test for the existence of a frontier, i.e., $H_{0}: \gamma=0$. As the alternative hypothesis is that $0<\gamma<1$, the test has an asymptotic distribution, the critical values of which are given by Kodde and Palm. If the hypothesis is accepted, then there is no evidence of technical inefficiency in the data and the production frontier is identical to a standard production function.

Several other standard tests are carried out on the specification of the production function and inefficiency distribution. As the basic model is assumed to be have a translog functional form, the hypothesis that the correct functional form of the model is Cobb-Douglas can be imposed by removing the squared and cross product terms from the translog production function, i.e., $\mathrm{H}_{0}: \beta_{i, k}=0$ and re-estimating the model. Distinguishing between a half normal and a truncated normal distribution as the most appropriate assumption for the inefficiency distribution can be undertaken by running the model under both assumptions. The half-normal distribution is a special case of the truncated normal distribution, and implicitly involves the restriction $\mathrm{H}_{0}$ : $\mu=0$. Similarly, the hypothesis that efficiency is invariant over time, i.e., $H_{0}: \eta=0$ can also be tested. The model is estimated first assuming time variant inefficiency, then restricted by modeling the frontier as time invariant.

The results of the specification tests indicate that the translog is the most appropriate functional form, that inefficiency exists, and that the most appropriate distributional assumption for the inefficiency is a truncated normal distribution with time varying inefficiency (Table 4).

The results for the translog models with the appropriate distributional characteristics are presented in Table 5. Most of the coefficients were found to be significant at the 1 per cent level.

The $\alpha$ coefficients are indicative of the elasticity of the output of the species chosen as the dependent variable with respect to the output of the other species and the inputs. A priori, it would be expected that the signs of these coefficients would be negative for the outputs of the other species, assuming some degree of substitution, and positive for the inputs. This was
found to be the case for both gear types, with the exception of haddock in the otter trawl model. For both gear types, the output elasticity with respect to days fished was close to unity, while the output elasticity with respect to engine power was less than one. This suggests constant returns with respect to days fished, but diminishing returns with respect to boat size.

The Allen elasticities of substitution between the key species were estimated at the means of the various inputs and outputs (Tables 6 and 7), following the approach proposed by Grosskopf et al.. A negative value of the elasticity indicates a substitute, while a positive value indicates a complement. The results suggest that substitution of some species is possible, but this is largely limited to 'bundles' of species. For example, for the beam trawlers, while the main target species is plaice, it appears possible to target sole to some degree. However, increasing sole output also increases the catch of anglerfish and 'other' species. Similarly, the fisher could increase the catch of cod, but also 'other' species. For the otter trawlers, there appears to be two available strategies, with cod, whiting and plaice being one group, and haddock, saithe, nephrops and 'other' being an alternative bundle.

In most cases, the potential of substitutability between the main species and the alternative species is relatively small. For example, while cod and haddock - the two main species - are substitutes for the otter trawlers, the elasticity of substitution is small, so the practical potential for substitution is limited. Similarly, the elasticity of substitution between sole and plaice - the two main species - for the beam trawlers is small, indicating only limited substitution potential. These results have profound consequences for regulations of these fisheries.

The elasticity of substitution between the main target species of each fleet segment (sole and plaice for beam trawl, cod and haddock for otter trawl) were also estimated for each observation in the data set. From these estimates, the average elasticity of substitution for each boat over the period of the data was calculated. An apparent relationship exists between the elasticity of substitution between sole and plaice and boat size (expressed in terms of engine power) for the beam trawl fleet (Figure 3a). Larger boats tended to have a more negative elasticity of substitution, whereas smaller boats tended to have more of a complementary relationship between the species. ${ }^{8}$ As larger boats are more mobile, they are better able to change fishing grounds and take advantage of different relative abundance of the species. In contrast, the smaller boats are more restricted in their movement, tending to fish in a more limited number of fishing grounds and consequently less able to adjust their output mix. Less of a difference was observed in the otter trawl fleet (Figure 3b). Around one quarter of the boats had, on average, a positive elasticity of substitution, and these tended to be the smaller boats in the fishery. However, a greater number of smaller vessels had negative elasticities, although these were also highly inelastic.

The estimated distributions of efficiency for the two fleet segments differed substantially (Figure 4). Over two thirds of the beam trawlers were more than 70 per cent efficient on average over the period of the data. In contrast, over 90 per cent of the otter trawlers were less than 70 per cent efficient on average.

From the model results (Table 5), average individual otter trawl efficiency increased by around 2.3 per cent a year. The removal and replacement of less efficient otter trawlers over the time period resulted in a slight additional increase in average efficiency for the fleet segment as a whole, with an average rate of efficiency increase of around 2.6 per cent (Figure
5). In contrast, average individual efficiency of the beam trawlers decreased by 6.5 per cent a year (Table 5), while removal of the lesser efficient vessels (and introduction of more efficient vessels into the panel) resulted in an overall average decline in the efficiency of the fleet segment of around 1 per cent.

A decline in average individual vessel efficiency of Dutch beam trawlers operating in the North Sea was also observed over the same period (Pascoe et al.). This was attributed to increased crowding pressure, as TACs for sole and plaice were reduced while fleet sizes remained relatively constant. For the UK fleet, total beam trawl numbers effectively halved over the period examined, reducing the potential increase in crowding externalities. However, as overall international pressure on these shared stocks did not decrease at the same rate, this would still have negatively impinged on the efficiency of the UK vessels.

## Policy Implications

Interactions between species in a fishery may be either biological, e.g. predator-prey, or technical, i.e., joint production. Technical interactions within fisheries have generally been assumed to exist, although the strength of the interaction has not been previously quantified. Moreover, implications for fisheries management have never before been investigated. Most previous studies of production functions and frontiers in fisheries have generally applied a composite output measure on the assumption that applying a set of inputs to a given set of fish stocks, usually expressed as a composite stock measure, results in a given level of total output. Alvarez and Orea examined both multi-output production functions and multi-output distance functions for two species (one being a composite bycatch 'species'), but did not extend their analysis to consider elasticities of substitution between the outputs.

Excluding the stock from the production frontier does not allow the effects of changes in stock size on targeting behavior to be examined. A high relative stock abundance of a species would result in its cost per unit capture decreasing (relative to the other species with lower stock abundances), and may encourage some change in targeting behavior, i.e., output substitution, if possible. However, high stock abundance resulting in high catches may also result in lower prices, so the incentives to change targeting behavior may be less than expected. In either case, these effects cannot be captured (and are effectively assumed to be zero) through the exclusion of stock. However, as the elasticity of substitution is a technical (rather than economic) measure, if these factors had influenced targeting behavior and had resulted in changes in output composition then they should have been identified through the interaction terms in the model. The fact that some substitution has been observed in the data may be a direct result of these factors.

The results of the study have implications for the continuing management of the fishery. In the European Union, as in most other countries, total allowable catches (TACs) are generally set on the basis of the status of the stock of the individual species rather than on the basis of the technical interactions between the species. This is particularly the case when stocks of some species are severely depressed, requiring substantial decreases in the allowable catch. In such cases, pressure is often placed on policy makers to increase the TACs of less biologically vulnerable species in order to reduce the impact of the reduced catch of the vulnerable species on fishermen's income.

In the case of the North Sea stocks, the technical interaction between haddock, cod and whiting, for example, has been recognized by fisheries scientists, and advice to policy makers has been to control the catches of these species in relation to each other (ICES). The decline
in the North Sea cod stock has resulted in substantial declines in allowable catches in a bid to avoid stock collapse and allow the stock to recover. In 2000, the North Sea cod stock was estimated to be roughly 20 per cent of the level of population of mature fish required for sound recruitment (the Bpa, or "Biomass according to the precautionary approach"). A "recovery program" was instigated with the aim of enabling the stock of mature fish to increase by 30 per cent a year until the Bpa level has been achieved. The TAC for cod in the North Sea was reduced from 81,000 tonnes in 2000 to 48,600 tonnes in 2001, and further reduced to 41,600 tonnes in 2002 (European Commission).

In contrast, North Sea TACs of both haddock and saithe were increased by 62 and 55 per cent respectively between 2001 and 2002. The increase in stock that is presumed to underly these TAC increases will result in an increased proportion of these species in the catch, ceteris paribus. However, stocks of these species are still considered low (ICES), and it is likely that the TAC increases are, in part, a means of 'softening' the impact of the decreased cod TACs. Given the limited substitutability between cod and haddock and also saithe, which is complementary to haddock, the disparity in the TACs may lead to increased discarding of over-quota cod, provided it is economically viable to continue fishing for haddock and saithe without the additional revenue derived from cod. ${ }^{9}$

For the beam trawl fleet, scientific advice for 2002 for the two main species was a 30 per cent reduction in the TAC of plaice and 20 per cent reduction in the TAC of sole in the North Sea (ICES 2001). Recognition was again given to the joint nature of the output of the two species in the scientific advice. Final changes in TACs were, in contrast, less than a 5 per cent decrease for plaice and 16 per cent for sole (European Commission). Again, given the limited substitutability between sole and plaice, the incompatible TACs may result in increased
discarding of sole. However, as sole is substantially more valuable on a per unit basis, it may not be economically viable for fishermen to land only plaice and discard sole, resulting in either the TAC for plaice not being filled, or providing incentives to land over-quota catch of sole illegally.

The results of the analysis also suggest that there is an apparent relationship between boat size and the ability to target individual species. This was more obvious in the beam trawl fleet, where the larger boats demonstrated a clear substitution relationship, while the smaller vessels in many cases had a complementary relationship. The ability to substitute catch for the otter trawlers was on average also relatively low, with the smallest boats also demonstrating complementarity. The majority of the otter trawlers were of similar size as the smaller beam trawlers, reinforcing this relationship between boat size and the ability to influence product mix.

An objection often raised in opposition of the use of individual transferable quotas (ITQs) is that quota tends to concentrate in the fishery in a smaller number of larger vessels. While this may have benefits in terms of economies of scale, the results of this study suggest that it is the larger vessels that are most able to adjust their product mix, and therefore be most able to respond to changes in the relative TACs. Restrictions on trade in quota that reduce concentration may be contributing to the other problem often associated with ITQs, namely over-quota catch and discarding. As the smaller vessels appear less able to adjust their catch mix, then changes in relative TACs will result in greater inconsistency between quota holdings and product mix unless the quota market is sufficiently flexible to allow fishers to adjust their quota holdings. The UK policy of fixed quota allocations inhibits the adjustment
of quota holdings. With limited ability to adjust both catch composition and quota holdings, incompatible TACs can only result in greater discarding or illegal landings.

The results of the study reinforce the need for fisheries managers to consider the technical interactions between species when setting the TACs. These interactions have been recognized by fisheries scientists, and have been generally assumed to exist by fisheries economists. However, this represents the first empirical analysis to quantify these interactions in the context of fisheries management. Failure to consider these interactions may result in increased discarding in the fishery, illegal fishing and potentially lower than expected future yields.

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## Footnotes

${ }^{1}$ See e.g. Kirkley, Squires and Strand 1995, 1998; Campbell and Hand; Sharma and Leung; Grafton, Squires and Fox; Alvarez; Pascoe, Anderson and de Wilde, Pascoe and Coglan; Herrero and Pascoe.
${ }^{2}$ Production technology is defined by output sets, $P(\mathbf{x})$, which represents the set of all output vectors, $\mathbf{y}$, which can be produced using the input vector, $\mathbf{x}$, i.e., $P(\mathbf{x})=\{\mathbf{y}: \mathbf{x}$ can produce $\mathbf{y}\}$. The properties of this set are summarised as follows: for each $\mathbf{x}$, the output set $P(\mathbf{x})$ is assumed to satisfy (i) 0 ? $P(\mathbf{x})$; (ii) non-zero output levels cannot be produced from zero level of inputs; (iii) $P(\mathbf{x})$ satisfies strong disposability of outputs: if $\mathbf{y}$ ? $P(\mathbf{x})$ and $\mathbf{y}^{*}=\mathbf{y}$ then $y^{*}$ ? $P(\mathbf{x})$; (iv) $P(\mathbf{x})$ satisfies strong disposability of inputs: if $\mathbf{y}$ can be produced from $\mathbf{x}$, then $\mathbf{y}$ can be produced from any $\mathbf{x}^{*}=\mathbf{x}$; (vi) $P(\mathbf{x})$ is bounded (which is essentially a mathematical requirement that implies that we cannot produce unlimited levels of outputs with a given set of inputs); (vii) $P(\mathbf{x})$ is convex (which implies that if two combinations of output levels can be produced with a given input vector $\mathbf{x}$, then any average of these output vectors can also be produced; this assumption implicitly requires the commodities to be continuously divisible).
${ }^{3}$ The properties of $D(\mathbf{x}, \mathbf{y})$ follow directly from the axioms on the technology set and play a major role in efficiency measurement: (i) $D(\mathbf{x}, \mathbf{y})$ is non-decreasing in $\mathbf{y}$ and increasing in $\mathbf{x}$; (ii) $D(\mathbf{x}, \mathbf{y})$ is linearly homogeneous in $\mathbf{y}$; (iii) if $\mathbf{y}$ belongs to the production possibility set of $\mathbf{x}$ (i.e., $\mathbf{y} \boldsymbol{?} P(\mathbf{x})$ ), then $D(\mathbf{x}, \mathbf{y})=1$; and (iv) distance is equal to unity (i.e., $D(\mathbf{x}, \mathbf{y})=1$ ) if $\mathbf{y}$ belongs to the "frontier" of the production possibility set.
${ }^{4}$ A number of fisheries are regulated with individual vessel quotas (IVQs), setting an upper bound on output per species per boat, in addition to a TAC for the entire fishery. The IVQs may or may not be tradable.
${ }^{5}$ Furthermore, since the TAC is given, if some vessels are to increase their output, others must reduce theirs. As argued by Asche et al., one can also obtain optimal fleet size, and therefore an indication of the overcapacity in the fishery. This is important information in fisheries managed with IVQs, as it will provide information about the extent to which one has been able to collect the resource rent and how much resource rent is dissipated due to overcapacity in the fishery.
${ }^{6}$ The definition of the output distance function uses $\min$ (minimum) instead of inf (infinum), implying the assumption of the absence of the possibility that the minimum does not exist (i.e., that ? $=+\infty$ is possible).
${ }^{7}$ This was not a problem for the beam trawl fleet as all UK beam trawlers operate out of English ports.
${ }^{8}$ This relationship was relatively weak statistically, with a correlation of $\mathrm{r}=-0.13$. This increased to $\mathrm{r}=-0.51$ if three of the large vessels with high positive elasticities were excluded.
${ }^{9}$ The economic incentives to discard fish has been well established in the literature. See for example Anderson; , Arnason; Pascoe.

Figure 1. North Atlantic fishing grounds. The North Sea is represented by ICES Division IV.


Figure 2: Relative stock indexes for a) beam trawl species and b) otter trawl species



Figure 3. Average elasticitity of substitution against engine power: a) sole and plaice, beam trawlers; and b) cod and haddock, otter trawlers



Figure 4. Distribution of average individual vessel efficiency over the period 1990-2000.


Figure 5. Average vessel efficiency over the period 1990-2000.


Table 1: TAC allocation for North Sea species ${ }^{\text {a }}$ (kt) and estimated value ${ }^{\text {b }}$ (mEuro), 1999

|  | Belgium | Denmark | France | Germany Netherlands | Norway | UK | Total | Value |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Demersal groundfish |  |  |  |  |  |  |  |  |  |
| Cod | 4.7 | 23.9 | 4.9 | 12.1 | 13.1 | 12.5 | 52.4 | 132.4 | 197.4 |
| Haddock | 0.8 | 5.2 | 5.8 | 3.3 | 0.4 | 14.9 | 56.0 | 88.6 | 90.9 |
| Whiting | 1.2 | 4.9 | 8.2 | 1.4 | 3.0 | 4.4 | 20.9 | 44.0 | 38.9 |
| Saithe | 0.1 | 2.3 | 13.3 | 6.5 | 0.0 | 57.2 | 4.5 | 110.0 | 84.7 |

Demersal flatfish

| Plaice | 6.1 | 14.9 | 0.6 | 6.1 | 46.6 | 3.4 | 23.8 | 102.0 | 132.9 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Sole | 1.6 | 1.1 | 0.3 | 1.2 | 14.9 | 0.0 | 0.9 | 20.3 | 131.0 |

## Invertebrates

| Nephrops | 0.8 | 0.8 | 0.0 | 0.1 | 0.4 | 0.0 | 12.9 | 15.2 | 79.5 |
| :--- | ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Other |  |  |  |  |  |  |  | 1688.4 | 704.7 |
| Total |  |  |  |  |  |  |  | 2200.9 | 1460.0 |

a) Allocation by country based on historical shares of TAC
b) Values based on guide prices for 1999
c) includes ICES Division IIa for some species

Table 2. Average characteristics and catch (kg) of key species, beam trawlers

| YEAR | Boats | Engine | Days | Plaice | Sole | Cod | Angler | Other |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | power (kW) |  |  |  |  |  |  |
| 1990 | 14 | 954 | 188 | 347,343 | 22,168 | 10,109 | 8,778 | 23,804 |
| 1991 | 27 | 791 | 156 | 194,968 | 15,038 | 6,711 | 6,430 | 20,054 |
| 1992 | 41 | 837 | 158 | 189,343 | 8,469 | 10,651 | 7,392 | 25,103 |
| 1993 | 43 | 815 | 178 | 191,841 | 7,247 | 14,440 | 10,688 | 35,899 |
| 1994 | 39 | 879 | 200 | 195,427 | 10,165 | 16,857 | 13,207 | 40,579 |
| 1995 | 41 | 842 | 196 | 187,727 | 9,697 | 13,557 | 12,184 | 38,977 |
| 1996 | 36 | 899 | 200 | 212,235 | 9,180 | 15,443 | 9,085 | 42,857 |
| 1997 | 38 | 891 | 191 | 238,279 | 4,163 | 14,526 | 11,150 | 44,008 |
| 1998 | 40 | 898 | 188 | 228,431 | 6,465 | 19,562 | 8,628 | 44,965 |
| 1999 | 39 | 898 | 181 | 190,520 | 7,168 | 13,918 | 6,175 | 37,716 |
| 2000 | 35 | 959 | 186 | 295,031 | 7,784 | 10,165 | 7,814 | 37,474 |

Table 3. Average characteristics and catch (kg) of key species, otter trawlers

| YEAR | Boats | Engine | Days | Cod | Haddock | Whiting | Saithe | Nephrops | Plaice | Other |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | power |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  | kW) |  |  |  |  |  |  |  |  |
| 1990 | 88 | 223 | 147 | 31,171 | 7,094 | 8,340 | 10,539 | 9,017 | 3,635 | 22,358 |
| 1991 | 96 | 217 | 140 | 28,662 | 6,209 | 7,959 | 13,992 | 7,739 | 3,701 | 19,590 |
| 1992 | 99 | 211 | 134 | 29,849 | 9,198 | 8,880 | 5,256 | 6,348 | 4,003 | 18,326 |
| 1993 | 111 | 217 | 141 | 30,841 | 12,666 | 9,964 | 11,149 | 11,199 | 2,651 | 15,493 |
| 1994 | 102 | 209 | 117 | 34,012 | 10,481 | 8,898 | 4,641 | 1,231 | 3,423 | 15,056 |
| 1995 | 110 | 212 | 118 | 36,883 | 11,484 | 8,036 | 10,946 | 859 | 4,140 | 15,572 |
| 1996 | 110 | 213 | 119 | 44,432 | 13,322 | 8,679 | 18,314 | 1,285 | 3,377 | 14,778 |
| 1997 | 124 | 206 | 121 | 38,443 | 14,757 | 11264 | 13,019 | 1,493 | 4,411 | 16,330 |
| 1998 | 123 | 211 | 142 | 62,507 | 15,709 | 13,479 | 10,847 | 1,623 | 3,636 | 15,286 |
| 1999 | 119 | 216 | 120 | 30,794 | 13,379 | 11,332 | 15,770 | 2,486 | 3,316 | 14,693 |
| 2000 | 104 | 229 | 122 | 22,601 | 10,964 | 10,377 | 10,048 | 3,691 | 4,352 | 13,427 |

Table 4. Specification tests
$\mathrm{L}\left(\mathrm{H}_{0}\right) \quad \mathrm{L}\left(\mathrm{H}_{1}\right) \quad \chi^{2} \quad$ Probability

## Beam trawl

| $\gamma=0$ | -163.578 | -100.621 | 125.915 | $<0.01 \%^{\mathrm{a}}$ |
| :--- | :---: | :---: | :---: | :---: |
| $\beta_{\mathrm{i}, \mathrm{j}}=0$ | -275.485 | -100.621 | 349.728 | $0.00 \%$ |
| $\mu=0$ | -102.542 | -100.621 | 3.841 | $5.00 \%$ |
| $\eta=0$ | -108.800 | -100.621 | 16.359 | $0.01 \%$ |

Otter trawl

| $\gamma=0$ | -687.097 | -481.432 | 411.331 | $<0.01 \%^{\mathrm{a}}$ |
| :--- | :---: | :---: | :---: | :---: |
| $\beta_{\mathrm{i}, \mathrm{j}}=0$ | -810.856 | -481.432 | 658.848 | $0.00 \%$ |
| $\mu=0$ | -490.692 | -481.432 | 18.521 | $0.00 \%$ |
| $\eta=0$ | -495.743 | -481.432 | 28.622 | $0.00 \%$ |

a) based on the one sided distribution tables developed by Kodde and Palm (1986)

Table 5. MLE results for the two fleet segments

|  | Beam trawl |  |  |  | Otter trawl |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Coeff | SE | t-stat |  | Coeff | SE | t-stat |
| Constant | 0.731 | 0.081 | 9.054*** | Constant | 1.024 | 0.082 | $12.411^{* * *}$ |
| Cod* | -0.036 | 0.024 | -1.531 | Haddock* | 0.121 | 0.012 | 9.752*** |
| Sole* | -0.233 | 0.016 | -14.331*** | Whiting* | -0.092 | 0.012 | -7.338*** |
| Angler* | -0.057 | 0.013 | -4.265*** | Saithe* | -0.064 | 0.008 | -8.016*** |
| Other* | -0.246 | 0.036 | -6.750*** | Nephrops* | -0.054 | 0.006 | -9.064*** |
| KW | 0.654 | 0.069 | 9.470 *** | plaice* | -0.129 | 0.015 | -8.561 *** |
| Days | 1.018 | 0.053 | 19.061*** | other* | -0.493 | 0.019 | -26.379*** |
| Cod** ${ }^{2}$ | -0.009 | 0.009 | -0.988 | KW | 0.835 | 0.068 | 12.358*** |
| Sole* ${ }^{2}$ | -0.012 | 0.003 | -3.758*** | Days | 0.978 | 0.029 | $33.691^{* * *}$ |
| Angler** | -0.012 | 0.003 | -4.560*** | Haddock*2 | 0.009 | 0.003 | 3.529 *** |
| Other** | -0.034 | 0.008 | -4.433*** | Whiting* ${ }^{2}$ | -0.006 | 0.002 | -3.582*** |
| KW ${ }^{2}$ | -0.036 | 0.094 | -0.383 | Saithe* ${ }^{2}$ | 0.002 | 0.001 | 1.604 |
| Days ${ }^{2}$ | 0.032 | 0.048 | 0.676 | Nephrops* ${ }^{2}$ | -0.001 | 0.001 | -1.047 |
| Cod*sole* | 0.008 | 0.012 | 0.639 | Plaice* ${ }^{2}$ | -0.010 | 0.003 | -4.000 *** |
| Cod*angler* | 0.008 | 0.009 | 0.823 | Other** | -0.016 | 0.005 | -3.220 *** |
| Cod*other* | -0.013 | 0.016 | -0.809*** | KW ${ }^{2}$ | 0.008 | 0.105 | 0.077 |
| Sole*angler* | -0.006 | 0.006 | -1.057 *** | Days ${ }^{2}$ | -0.011 | 0.026 | -0.415 |
| Sole*other* | -0.041 | 0.013 | -3.220 | Had*wht* | -0.015 | 0.004 | -4.107*** |
| Angler*other* | 0.027 | 0.010 | 2.783 | Had*saithe* | 0.015 | 0.004 | 4.086*** |
| Kw days | -0.041 | 0.058 | -0.704 | Had*nep* | 0.003 | 0.002 | 1.821* |
| Kw cod* | 0.000 | 0.036 | 0.008 | Had*plaice* | -0.015 | 0.005 | -3.086*** |
| Kw sole* | 0.168 | 0.024 | 6.904*** | Had*other* | 0.023 | 0.006 | $3.468 * * *$ |
| Kw ang* | 0.018 | 0.014 | 1.270 | whit*saithe* | 0.000 | 0.003 | 0.065 |
| Kw other* | -0.241 | 0.045 | $-5.389 * * *$ | Whi*neph* | 0.003 | 0.002 | 1.219 |
| Days cod* | 0.040 | 0.036 | 1.108 | Whi*plaice* | 0.002 | 0.003 | 0.868 |
| Days sole* | -0.057 | 0.021 | -2.682*** | Whi*other* | 0.017 | 0.004 | 3.945 *** |
| Days ang* | -0.043 | 0.016 | $-2.679 * * *$ | Saithe*nep* | 0.000 | 0.001 | 0.446 |
| Days other* | 0.075 | 0.037 | 2.047** | saithe*plaice* | 0.007 | 0.004 | 1.756* |
| $\sigma^{2}$ | 2.650 | 0.830 | $3.192 * * *$ | Saithe*other* | -0.039 | 0.005 | -7.811*** |
| $\gamma$ | 0.974 | 0.008 | 115.683*** | Nep*plaice* | 0.007 | 0.003 | 2.111** |
| $\mu$ | -3.214 | 0.616 | $-5.221 * * *$ | Nep*other* | -0.021 | 0.004 | $-4.845^{* * *}$ |
| $\eta$ | -0.065 | 0.014 | -4.726*** | plaice*other* | 0.023 | 0.005 | 4.133*** |
|  |  |  |  | Kw days | -0.045 | 0.067 | -0.671 |
|  |  |  |  | Kw had* | -0.095 | 0.024 | -4.029*** |
|  |  |  |  | Kw whi* | 0.050 | 0.020 | $2.542 * *$ |
|  |  |  |  | Kw saithe* | 0.005 | 0.013 | 0.340 |
|  |  |  |  | Kw neph* | 0.037 | 0.013 | $2.775^{* * *}$ |
|  |  |  |  | Kw plaice* | 0.023 | 0.026 | 0.862 |
|  |  |  |  | Kw other* | 0.077 | 0.028 | 2.753 *** |
|  |  |  |  | Days had* | 0.046 | 0.011 | $4.321^{* * *}$ |
|  |  |  |  | Days whi* | -0.015 | 0.013 | -1.154 |
|  |  |  |  | Days saithe* | 0.022 | 0.008 | 2.789*** |
|  |  |  |  | Days neph* | -0.021 | 0.006 | -3.251*** |
|  |  |  |  | Days plaice* | -0.020 | 0.017 | -1.174 |
|  |  |  |  | Days other* | -0.037 | 0.018 | -2.050** |
|  |  |  |  | $\sigma^{2}$ | 0.240 | 0.025 | 9.539*** |
|  |  |  |  | $\gamma$ | 0.617 | 0.030 | 20.634*** |
|  |  |  |  | $\mu$ | 0.770 | 0.067 | 11.427*** |
|  |  |  |  | $\eta$ | 0.023 | 0.004 | 5.604*** |

[^1]Table 6. Elasticity of substitution: beam trawl

|  | Plaice | Sole | Cod | Angler | Other |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Plaice | - |  |  |  |  |
| Sole | -0.373 | - |  |  |  |
| Cod | -0.291 | -0.659 | - | - |  |
| Angler | 0.465 | 0.346 | -2.653 | -1.391 |  |
| Other | -1.808 | 0.513 | 1.026 |  |  |

Table 7. Elasticity of substitution: otter trawl

|  | Cod | Haddock | Whiting | Saithe | Nephrops | Plaice | Other |
| :--- | ---: | ---: | :--- | :---: | :---: | :---: | ---: |
| Cod | - |  |  |  |  |  |  |
| Haddock | -0.247 | - |  |  |  |  |  |
| Whiting | 0.029 | -0.570 | - |  |  |  |  |
| Saithe | -0.347 | 0.820 | -0.016 | - |  |  |  |
| Nephrops | -0.247 | 0.214 | -0.237 | -0.053 |  |  |  |
| Plaice | 0.281 | -0.411 | -0.083 | -0.370 | -0.448 | - |  |
| Other | -0.043 | 0.164 | -0.163 | 0.542 | 0.345 | -0.154 |  |


[^0]:    ${ }^{1}$ Address for correspondence: Dr. Phoebe Koundouri, The University of Reading, School of Business, Department of Economics, HUMSS Building, PO Box 218, Whiteknights, Reading, RG6 6AA, Berkshire, UK. Tel. + 44 (0) 118378 7862; Fax. +44 (0) 118975 0236; e-mail: p.koundouri@reading.ac.uk

    Trond Bjornal is a Visiting Professor in the Centre for the Economics and Management of Aquatic Resources (CEMARE), Department of Economics, University of Portsmouth. Phoebe Koundouri is a Lecturer in the Department of Economics at the University of Reading, and a Senior Research Fellow in the Centre for Socio-Economic Research on the Global environment (CESERG), Department of Economics, University College London. Sean Pascoe is a Professor in CEMARE, Department of Economics, University of Portsmouth. Authorship is in alphabetical order.

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[^1]:    *** significant at the $1 \%$ level; ** significant at the 5\% level; * significant at the $10 \%$ level.

